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## Some Observations on Zap and Its Applications

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Abstract. In this paper we make some observations on the zaps and their applications developed by Dwork and Naor [13]. We clarify the relations among public-coin witness indistinguishability (WI), public-coin honest verifier zero-knowledge (HVZK) and public-coin special honest verifier zero-knowledge (SHVZK). Specifically, we observe that the existence of zaps under the existence of one-way permutations actually strictly separates public-coin WI and public-coin SHVZK assuming  $\mathcal{NP} \not\subseteq \mathcal{BPP}$ . We also show that public-coin HVZK does not implies WI assuming the existence of one-way permutations. For zap-based applications, we present an improved Dwork-Naor 2-round timed deniable authentication scheme that improves the communication and computation complexity of the original protocol presented by Dwork and Naor [13]. Specifically, in the improved protocol the first message (from the verifier to the authenticator) is independent on the message to be authenticated by the authenticator.

**Keywords.** cryptography, interactive proof systems, zap, deniable authentication, software copyright protection

## 1 Introduction

Zap, first introduced by Dwork and Naor [13], is itself a 2-round public-coin witness indistinguishable (WI) proof system for  $\mathcal{NP}$ . Zaps are a very powerful cryptographic tool to significantly simplify many cryptographic tasks. As a notable example, it is used to achieve the first 2-round timed deniable authentication scheme [13].

Deniable authentication first appears in [10, 12], and is then formalized in [14]. Roughly speaking, a deniable authentication scheme is a *public-key interactive* authentication scheme in which an authenticator AP convinces a second party V, only accessing to AP's public-key, that AP is willing to authenticate a message m. However, different from the case of digital signatures, deniable authentication does not permit V to convince a third party that AP has authenticated m. That is, there is no "paper trail" of the conversation other than what could be produced by V alone. Several 4-round timed deniable authentication protocols appear in [14, 15] and the first 2-round timed deniable authentication is presented by Dwork and Naor in [13].