Dynamics of Continuous, Discrete and Impulsive Systems Series A: Mathematical Analysis 16 (2009) 209-219 Copyright ©2009 Watam Press

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ON POSITIVE SOLUTIONS OF NONLINEAR TELEGRAPH SEMIPOSITONE SYSTEM

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Abstract. In this paper, we shall deal with the superlinear semipositone problem of a nonlinear telegraph system and establish the existence of positive doubly periodic solutions for the system. The proofs are based on a fixed-point theorem in cones.

Keywords. Telegraph system, semipositone problem, doubly periodic solution, cone, fixed point theorem.

AMS (MOS) subject classification: 35B15, 47H10.

1 Introduction

In this paper we are concerned with the existence of positive doubly periodic solutions for the nonlinear telegraph system

$$\begin{cases} u_{tt} - u_{xx} + c_1 u_t + a_1(t, x)u = b_1(t, x)f(t, x, u, v), \\ v_{tt} - v_{xx} + c_2 v_t + a_2(t, x)v = b_2(t, x)g(t, x, u, v), \end{cases}$$
(1)

with doubly periodic boundary conditions

$$u(t+2\pi, x) = u(t, x+2\pi) = u(t, x), \quad (t, x) \in \mathbb{R}^2, v(t+2\pi, x) = v(t, x+2\pi) = v(t, x), \quad (t, x) \in \mathbb{R}^2.$$
(2)

where $c_1, c_2 > 0$ are constants, $a_i(t, x), b_i(t, x) \in C(R^2, R^+), f(t, x, u, v), g(t, x, u, v) \in C(R^2 \times R^+ \times R^+, R)$ and $a_i(t, x), b_i(t, x), f(t, x, u, v), g(t, x, u, v)$ are 2π -periodic in t and x.

The existence of doubly periodic solutions for a single telegraph equation is studied by many authors when the nonlinear is bounded or linear growth, see [1]-[6]. The first maximum principle for linear telegraph equations was built by Ortega and Robles-Perez in [5]. They proved the maximum principle for the doubly 2π -periodic solutions of the linear telegraph equation

$$u_{tt} - u_{xx} + cu_t + \lambda u = h(t, x), \quad (t, x) \in \mathbb{R}^2,$$