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ON LIAPUNOV-TYPE INTEGRAL INEQUALITIES FOR THIRD ORDER DYNAMIC EQUATIONS ON TIME SCALES

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Abstract. In this paper, Liapunov-type integral inequalities has been obtained for third order dynamic equations on time scales by using elementary analysis. A criterion for disconjugacy of third order dynamic equation is obtained in an interval $[a, \sigma(b)]$.

Keywords. Liapunov-type inequality, disconjugacy, third order dynamic equations.

AMS (MOS) subject classification: 34 C 10, 34 N 05.

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